

reducing imbalance penalties. The optimal forecast in this application is not necessarily the one that minimises the Mean Absolute Percentage Error (MAPE), but rather the one that minimises financial losses.

If the costs π_{t+h}^+ and π_{t+h}^- are independent from d_{t+h}^r and positive, the quantile minimizing this equation can be calculated analytically using formula in Equation (4):

$$\tau_{t+h}^{opt} = \frac{\pi_{t+h}^+}{\pi_{t+h}^+ + \pi_{t+h}^-} \quad (4)$$

DLR Forecast optimised quantile

The method described above is here adapted to DLR forecasting. We consider that a quantile forecast of the DLR, $\hat{Y}_{t+h|t}^r$ can be calculated. In this case, both $\hat{Y}_{t+h|t}^r$ and d_{t+h}^r are expressed in MVA. The DLR is considered as the thermal limit of the line, although this value should be reduced by taking into account other criteria due to grid limitations, for example: i) the limited size of balancing reserves on both sides of the line, ii) the risk of removing N-1 configurations in case a DLR forecast appears to be false, iii) the current stability limits, and iv) the thermal limits of other components, such as circuit breakers or transformers. However, for the sake of simplicity, these constraints are not considered in this study.

The following study is carried out for a line connecting two different electricity markets. The case study was designed to express simply the financial cost at both sides of the line due to errors related to DLR forecasting. As a reminder, as described in [12], a producer participating in an electricity market can go through four channels:

- The electricity futures market, on which long-term contracts on electricity bids are made.
- The day-ahead market, also called the spot market, on which a unique spot price is set depending on the proposed bids.
- The intraday market, on which the imbalances that occurred during the day can be corrected. This usually ends from 30 minutes to 2 hours before the time of delivery.
- Towards the end of the intraday market and the delivery time, possible imbalances are corrected during balancing by the transmission system operator. Positive and negative imbalances can have different costs.

The economic benefits associated with DLR forecasts are here considered to be dependent from the spot and imbalance costs. This involves assuming that the DLR forecast error has a different financial cost for positive and negative errors:

- If $d_{t+h}^r > 0$, for a line connecting two areas with different spot electricity costs, C_t^1 and C_t^2 (€/MW),

the following cost is defined in Equation (5):

$$\pi_{t+h}^+ = -|C_t^1 - C_t^2| \quad (5)$$

This cost is linked to the fact that a better forecast would have increased the economic benefits relative to the use of the line. It is assumed that the increased rating of the line has no impact on C_t^1 and C_t^2 .

- If $d_{t+h}^r < 0$, the rating of the line is reduced to Y_{t+h}^+ , and up and down reserves are activated in the two connected areas. If $C_t^1 > C_t^2$, it causes a cost described in Equation (6). In the opposite case, the indexes need to be swapped:

$$\pi_{t+h}^- = (C_t^{imbalance\ 1^-} + C_t^{imbalance\ 2^+}) \quad (6)$$

where $C_t^{imbalance\ 1^-}$ is the regulation cost for negative imbalances in the first area. $C_t^{imbalance\ 2^+}$ is the regulation cost for positive imbalances in the second area. It is supposed that both these parameters are independent from d .

At this point, considering (4), (5) and (6), the quantile optimising the financial benefits from DLR forecast can be calculated as in Equation (7):

$$\tau_{opt} = \frac{|C_t^1 - C_t^2|}{|C_t^1 - C_t^2| + C_t^{imbalance\ 1^-} + C_t^{imbalance\ 2^+}} \quad (7)$$

CASE STUDY

The test case considered here is a virtual line at the border of France and Belgium, connecting the two countries. It is located at the position (3.125°N, 50.375°E, only one point was considered in this study and not the whole length of the circuit), and was studied from 1st January 2014 to 31st December 2015. We considered that the line is equipped with a 175mm² Lynx conductor.

The spot prices for France were provided by EPEX and those for Belgium by BELPEX. The balancing cost data were provided by the two national transmission system operators, RTE and Elia.

The DLR was calculated every 12 hours at the studied position, using reanalysis data provided by the European Center for Medium range Weather Forecasts (ECMWF) and the CIGRE standard method for calculating DLR [2]. The parameters used were:

- The 10m East/West wind component Uf (m.s⁻¹).
- The 10m North/South wind component Vf (m.s⁻¹).
- The ambient temperature Tf (°C).
- The solar radiation S set equal to 0 W.m⁻².

The DLR forecasts were generated using Numerical Weather Predictions (NWP) provided by ECMWF for the same parameters, at 4 positions close to the studied point. The prediction horizon h of the forecasts was equal to 24 hours. The forecasts were provided with a Quantile Regression Forest method (QRF) [13], which

was trained with the data from 2014. Data from 2015 was used for the evaluation.

RESULTS

DLR forecasts

Day-ahead DLR forecasts were provided every 12 hours for the studied case, and the 99 percentiles associated with the forecasted DLR were calculated. As an example, the result obtained for one month is shown in Figure 1.

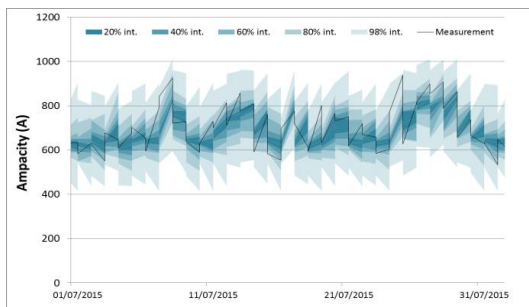


Figure 1. Consecutive day-ahead DLR forecasts from 01/07/2015 to 31/07/2015.

Using the MAPE, we can compare the deterministic performances of the model with the ones of a persistence model, whereby the forecast made at t for $t + h$ is equal to the observation at t . A MAPE of 8.1% was calculated for the QRF, and of 11.4% for the persistence model.

Optimised quantile

Two methods were proposed for the quantile selection:

- An arbitrarily selected quantile $\tau_{\text{Arbitrary}}$.
- A dynamically modified quantile in accordance with the spot prices, selected using Equation (7). Depending on the values of the balancing costs used, two quantiles are calculated: τ_{Spot} with the mean balancing cost values of the same month during the previous year and $\tau_{\text{Spot,Balancing}}$ with observed balancing costs at time $t + h$.

For the first method, the economic benefits linked to the current flowing through the lines were calculated for various quantiles, from 1% to 100%. As seen on Figure 2, the benefits were optimised using the 14%-quantile. This evaluation was made with the formula in Equation (8).

$$z = \min(\hat{Y}_{t+h|t}^{\tau}, Y_{t+h}) * |C_t^{SPOT,1} - C_t^{SPOT,2}| + \max(\hat{Y}_{t+h|t}^{\tau} - Y_{t+h}, 0) * (C_t^{\text{imbalance } 1^-} + C_t^{\text{imbalance } 2^+}) \quad (8)$$

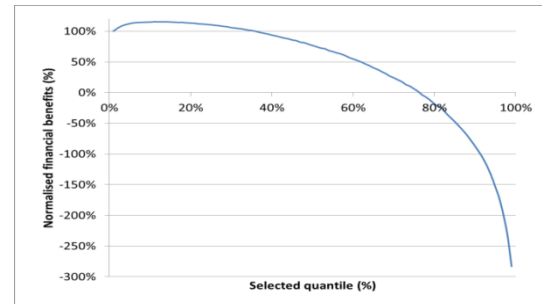


Figure 2. Benefits with an arbitrarily selected quantile

With the second method, the quantiles were calculated for 2015. The mean values for each month were provided in Table 1.

Parameter	τ_{Spot}	$\tau_{\text{Spot,Balancing}}$
January	2.5%	2,6%
February	2.8%	2,1%
Mars	4.1%	3,8%
April	10.9%	10,8%
May	12.9%	14,7%
June	8.7%	8,0%
July	7.4%	8,0%
August	10.2%	8,8%
September	15.2%	18,2%
October	9.3%	8,6%
November	3.9%	4,9%
December	2.5%	7,6%
Mean value	7.5%	8.2%

Table 1. Mean optimal quantile selected during 2015.

In order to evaluate the financial benefit of the proposed approaches, 5 cases were tested and compared:

1. The 1%-quantile DLR forecasts were used.
2. The 50%-quantile DLR forecasts were used.
3. The $\tau_{\text{Arbitrary}}$ -quantile DLR forecasts were used. $\tau_{\text{Arbitrary}}$ is set as equal to 14%.
4. The τ_{Spot} -quantile DLR forecasts were used.
5. The $\tau_{\text{Spot,Balancing}}$ -quantile DLR forecasts were used.

The benefits achieved during 2016 for the five cases were compared and the results are shown in Table 2. The results were normalised with respect to the benefits achieved using an arbitrary 1% quantile.

Case	Financial benefits respect to 1%
1%-forecasts	100.0%
50%-forecasts	76.7%
$\tau_{\text{Arbitrary}}$ -forecasts	115.1%
τ_{Spot} forecasts	115%
$\tau_{\text{Spot,Balancing}}$ forecasts	120.2%

Table 2. Normalized benefits for cases 1 to 5

The analysis of these results leads to the following considerations:

- Using an arbitrary 50%-quantile of the forecasts was counter-productive.
- Increasing the chosen quantile from 1% to 14% increased the financial benefits by 15.1%.

- The choice of a variable optimal quantile taking into account spot prices and historical average balancing costs increased the benefits by 15.0%. If real balancing costs at $t+h$ were taken into account, the benefits increased by 20.2%.

CONCLUSIONS

The study presented a methodology for selecting the optimal quantile to determine a forecast DLR obtained using probabilistic methods. The methodology is based on a cost-benefit analysis and the aim is to use it, along with other criteria, to optimize day-ahead DLR forecasts.

The methodology proposed was tested on a test case describing a circuit on which DLR is applied, connecting two electricity market zones with different prices and balancing costs. This case is simple, and more complex situations should be studied further, but the observed results are promising and show potential benefits compared to the standard method using an arbitrarily selected low quantile.

It should be stressed that whilst the choice of the quantile is not influenced by the actual value of the rating, the financial benefit calculated is. This means that the results presented in Table 2 are more dependent on the data used, and in particular on the meteorological data used for rating calculations and forecasts, which are obtained from 12-hour reanalysis. The use of more precise historical weather data is expected to increase the precision of the forecasts and the results, but also to increase the variability of the rating. Moreover, this methodology based on a simple cost-benefit analysis does not take into account other DLR limitations, which should be included in further studies on adapting DLR forecasts to grid conditions. Other criteria, such as the costs associated with increased risks, could be considered when evaluating DLR forecast errors.

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